

Introduction

Numerical Methods

Cezar Santos

FGV/EPGE

Some Info

- ▶ **This course:** Provides techniques for the analysis and evaluation of dynamic economic models, e.g. DSGE, firm and industry models
- ▶ The main emphasis is on learning the computational tools and their implementation
- ▶ **Target group:** Students who intend to do quantitative research in macro, applied micro or structural econometrics
- ▶ Requires you to use standard computer programming languages (such as Matlab, C or Fortran)
- ▶ **Background:** Dynamic programming / Recursive macro

Why Study Numerical Methods?

- ▶ “Paper-and-pencil” has its limits
- ▶ Often closed form solutions to models are hard or impossible to obtain
- ▶ Increasing computational power allows to study complex models
- ▶ Techniques also useful for fields that require structural modeling (and estimation), e.g. applied microeconomics
- ▶ Macro:
 - ▶ Dynamic general equilibrium models: Keystone of modern macroeconomics
 - ▶ Provides powerful tool for evaluating macroeconomic theories, macroeconomic policy, welfare
 - ▶ “Quantitative”: Provides ways in which to evaluate the empirical plausibility of the theory
 - ▶ Need to have the tools to analyze and compute dynamic economic models
- ▶ Drawbacks: Only approximate solution, no theorems/proofs, plenty of room for human error ...

What About Knowledge of Computers?

- ▶ In order to implement the techniques we're gonna cover, you need to learn (at least) one programming language
- ▶ Interpreted vs compiled languages
 - ▶ Interpreted: Matlab, Mathematica, Python, etc.
 - ▶ Compiled: Fortran, C, etc.
 - ▶ JIT (just-in-time) compilation: Julia
- ▶ Comparison:
 - ▶ Compiled is faster and easier to spot errors before the code is run
 - ▶ Check out this comparison: **Table 1**
 - ▶ Interpreted is much more flexible; easier to code
 - ▶ Compiled is much more verbose
- ▶ Basic principle: minimize *total* time

Getting Things Ready on YOUR Computer

- ▶ Interpreted languages:
 - ▶ Usually not much to do here; just install them
 - ▶ Note: Octave is a software that is essentially compatible with Matlab. Plus, it's free
 - ▶ Built-in IDEs: JuliaPro, Matlab, etc.
- ▶ Compiled languages:
 - ▶ Usually easier to set up on Unix based machines (Mac or Linux)
 - ▶ You first need a compiler in order to run things
 - ▶ Intel Fortran or GNU Fortran (gfortran)
 - ▶ Both Intel and the GNU project (gcc) have C compilers
 - ▶ Most economists prefer Fortran
 - ▶ Good code editor
 - ▶ Mac: gedit, textwrangler, Notepad++, etc
 - ▶ IDE vs command line
 - ▶ Open source IDE: Visual Studio Code

Some Helpful Material

- ▶ We're not gonna follow any book in particular, but you may find the following references helpful:
 - ▶ Adda and Cooper, Dynamic Economics (**Amazon link**)
 - ▶ Judd, Numerical Methods in Economics (**Amazon link**)
 - ▶ Marimon and Scott, Computational Methods for the Study of Dynamic Economies (**Amazon link**)
 - ▶ Sauer, Numerical Analysis (**Amazon link**)
- ▶ Programming languages:
 - ▶ McConnell, Code Complete (**Amazon link**)
 - ▶ Gilat, Matlab: An Introduction (**Amazon link**)
 - ▶ Ellis, Philips and Lahey, Fortran 90 (**Amazon link**)
 - ▶ Fortran tutorials: **Link here** or **Grey's slides**

Some Helpful Material (cont.)

- ▶ Some economists with helpful stuff online:
 - ▶ Jesus Fernandez-Villaverde: **Link**
 - ▶ Grey Gordon: **Link**
 - ▶ Quantitative Econ: **Link**
- ▶ Tony Smith's tips: **Link**
- ▶ Alan Miller's Fortran software: **Link**

Our Running Example for a Good Chunk of the Course

- ▶ Standard RBC model
- ▶ Representative agent with preferences

$$E \sum_{t=0}^{\infty} \beta^t u(c_t)$$

- ▶ Representative firm with CRS technology subjective to multiplicative TFP shocks: $Y_t = z_t F(K_t, L_t)$
- ▶ No government
- ▶ Competitive equilibrium
- ▶ By the welfare theorems, we'll work with the planner's problem

Our Example: Recursive Formulation

- ▶ Since there's no utility for leisure, let's forget about it and define $f(k) = F(k, 1)$
- ▶ The (basic) problem we'll be trying to solve can be written as:

$$V(k, z) = \max_{c, k'} u(c) + E\beta V(k', z')$$

s.t.

$$c + k' = zf(k) + (1 - \delta)k$$

- ▶ Question: how to solve this problem?

Different Methods

- ▶ We'll discuss several different methods to solve the problem above (and, obviously, a lot more)
- ▶ Each method may be more suited for certain types of problems
- ▶ Some methods:
 - ▶ Value function iteration
 - ▶ Projection methods (spectral, finite elements)
- ▶ We'll also need to learn several helpful things:
 - ▶ root-finding, interpolation, discretization of stochastic processes, etc.
- ▶ We'll also discuss some techniques for some potentially more complicated models:
 - ▶ Computing stationary distributions, idiosyncratic and aggregate risk, OLG, calibration, simulation-based estimation, continuous-time models, etc.